Radiative Processes in Astrophysics Problem Set 4

Due date: Tuesday, 13 May 2003 at 10:15

1. Plane-parallel atmospheres

- (a) Why are plane-parallel layers often assumed for stellar atmospheres? Can you guess when this approximation is good and when not?
- (b) Explain how one gets the radiative transport equation and its formal solution in the case of a plane-parallel atmosphere. Include a sketch showing the geometry.

2. Eddington-Barbier approximation and limb darkening

- (a) What is the Eddington-Barbier approximation? Explain what assumptions went into deriving it, and what it means. Why is it useful?
- (b) What do we mean by "limb darkening"? Use Eddington-Barbier to explain this phenomenon.
- (c) Pretend that you have measured limb darkening observationally, and make plot(s) of your results. What would cause a limb *brightening* effect?

3. Bremsstrahlung example

Consider a sphere of ionized hydrogen plasma that is undergoing spherical gravitational collapse. The sphere remains at constant isothermal temperature T_0 , uniform density and constant mass M_0 during the collapse, and has decreasing radius R(t). The sphere's luminosity comes from bremsstrahlung radiation in its interior. Initially, at time $t = t_0$, the sphere is optically thin.

- (a) What is the total luminosity of the sphere as a function of M_0 , R(t) and T_0 while the sphere is optically thin?
- (b) What is the luminosity of the sphere as a function of time after it becomes optically (very) thick?
- (c) Draw a qualitative curve of the luminosity as a function of time and *interpret* this graph.